

OSU~EmEa – 6

# Static Energy Accounting

Emergy algebra, Emergy evaluation  
procedure , Static calculation

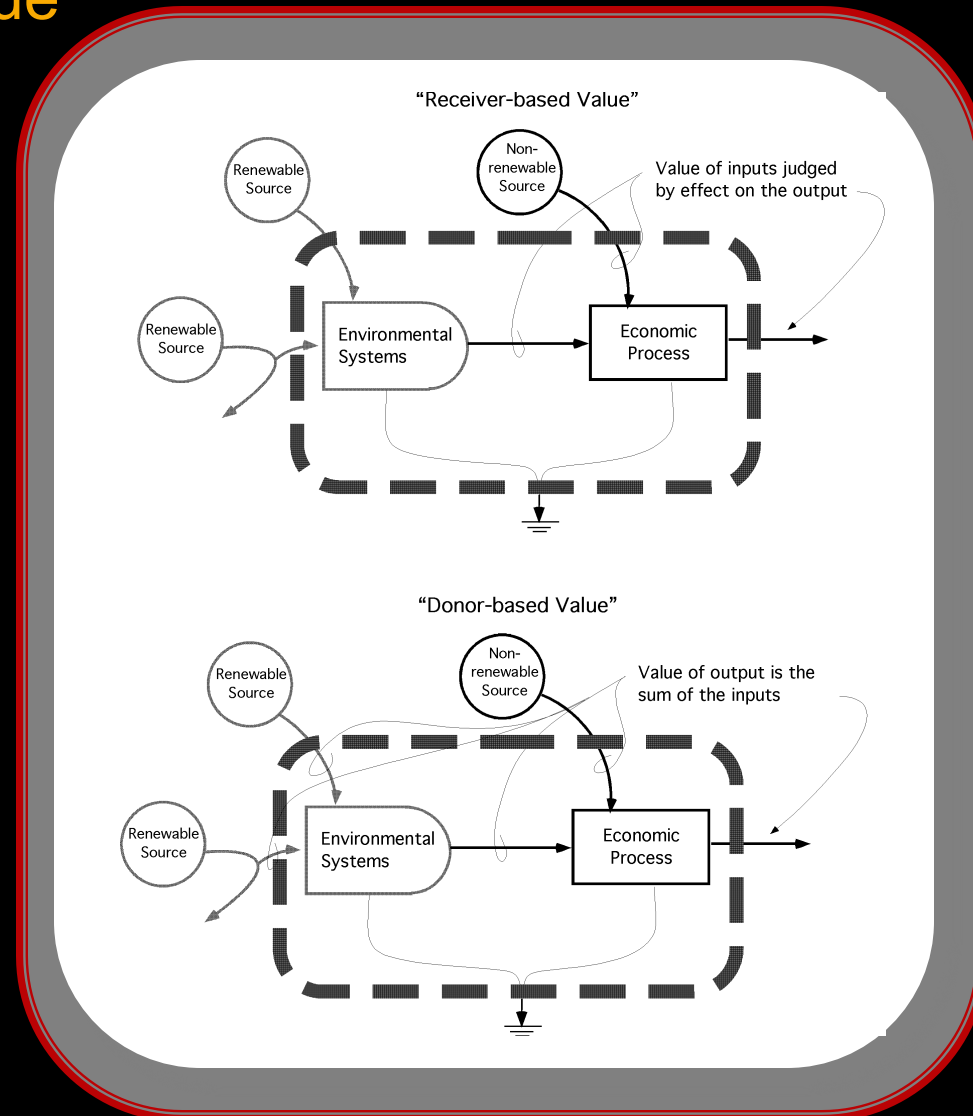
Six general rules for allocating energy within systems of processes....

and some interesting theoretical observations

## Donor Value vs. Receiver Value

Receiver Value = Utility theory of value....Classical economic value theory. "Willingness to pay"

Donor Value = Supply side perspective...what goes into something determines its value



Under a steady state assumption there are some general rules or accounting procedures that we have collectively called *Energy Algebra* (Odum, 1996).

The rules are used to assign energy to flows of energy, materials, and information within systems.

The first four rules describe how to assign energy to outputs including splits and co-products.

The fifth rule deals with double counting a special issue in static energy algebra to insure that feedbacks, recycle and co-products are treated correctly to avoid double counting.

The sixth rule pertains to by-product flows

In describing the rules mathematically,  
the following notations are used...

$u_i$  =  $i^{\text{th}}$  input flow, used

$Y_i$  =  $i^{\text{th}}$  output flow

$E(u_i)$  = available energy of the  $i^{\text{th}}$  input, used

$E(Y_i)$  = available energy of the  $i^{\text{th}}$  output,

$Em(u_i)$  = energy of the  $i^{\text{th}}$  input,

$Em(Y_i)$  = energy of the  $i^{\text{th}}$  output,

$Tr_i$  = transformity of  $i^{\text{th}}$  flow or product,

$Sp_i$  = specific energy of  $i^{\text{th}}$  flow or product,

$UEV_i$  = unit energy value of  $i^{\text{th}}$  flow or product, and

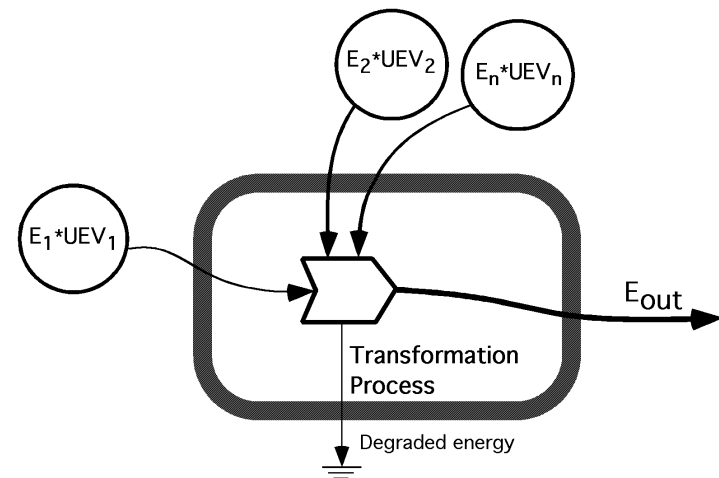
$\tilde{\Rightarrow}$  = “assigned to”

## Rule #1 – Definition of emergy

*Emergy is the available energy (exergy) of one kind that is used up in transformations directly and indirectly to make a product or service.*

The emergy of the output is equal to the sum of the inputs multiplied by their UEVs

The UEV of an output is equal to the emergy of the output divided by the energy or mass of the output.



$$E_{m_{out}} = \sum_1^n E_i * UEV_i$$

$$UEV = E_{m_{out}} / E_{out}$$

Where;

$E_{1...n}$  = Available energy inputs

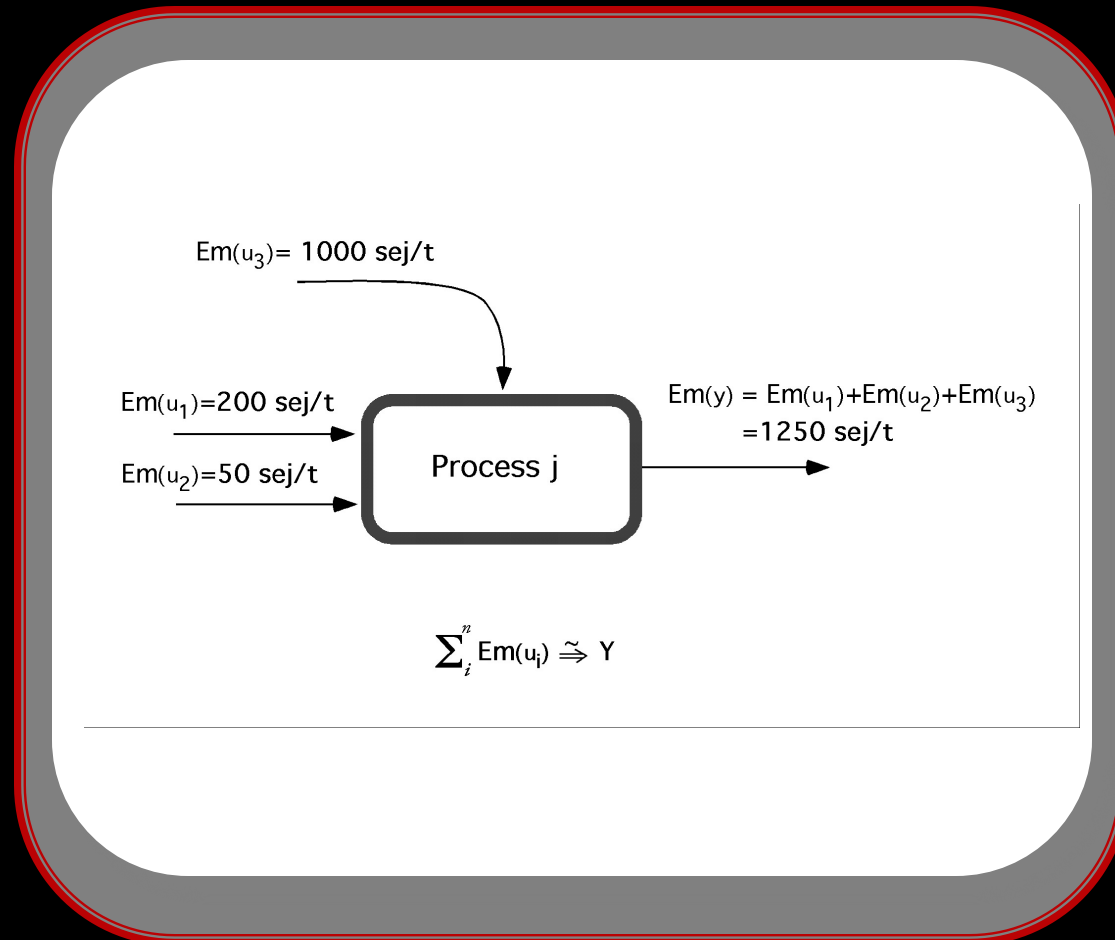
$E_{out}$  = Available energy of the output

$E_m$  = Emergy

UEV = Unit Emergy Value

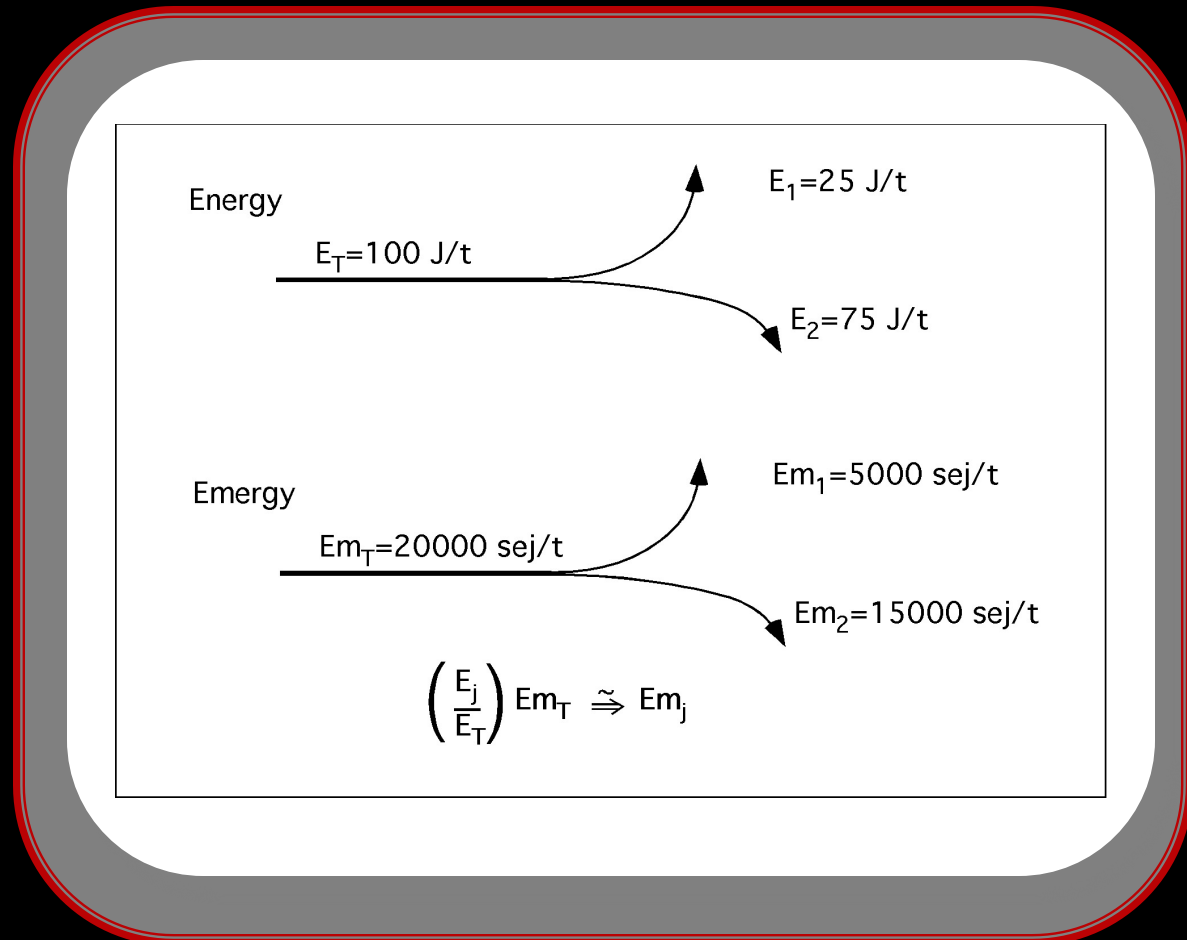
## Rule #2 – Assigning energy to transformation outputs

*In processes having one output, all independent energy inputs are assigned to the processes' output.*



## Rule #3 - Splits of the same material or energy...

*When a pathway splits, the energy is assigned to each branch of the split based on its percent of the total available energy flow (or mass) on the pathway before the split.*

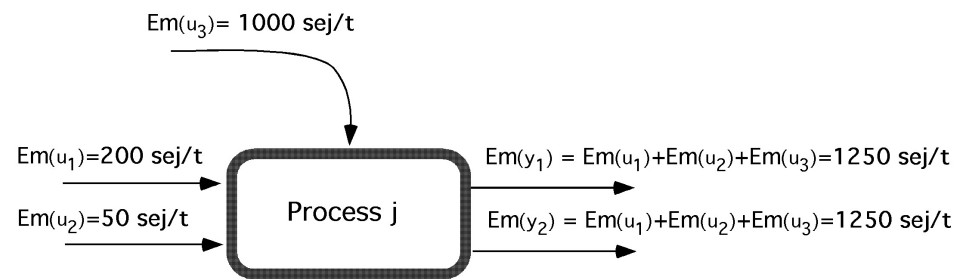




## Rule #4- Co-Products...

*In processes having two or more co-products, all independent input energy is assigned to each co-product.*

*A **co-product** is a product that is produced jointly with another product*



$$\sum Em(u_i) \Rightarrow \forall Y_i \in \{Y_1, \dots, Y_n\}$$

$\forall$  = to all

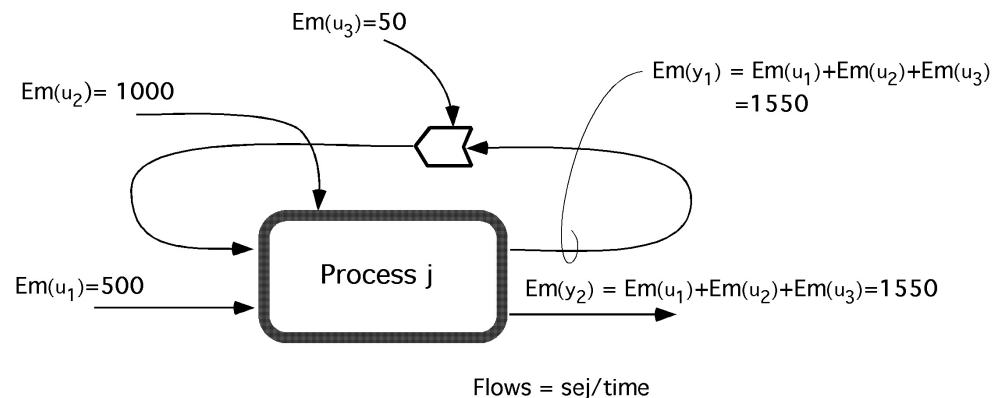
$Y_i$  =  $i^{\text{th}}$  co-product

$\in$  = belonging to the set

## Rule #5 – Double counting...

*Within a system, energy cannot be counted twice:*

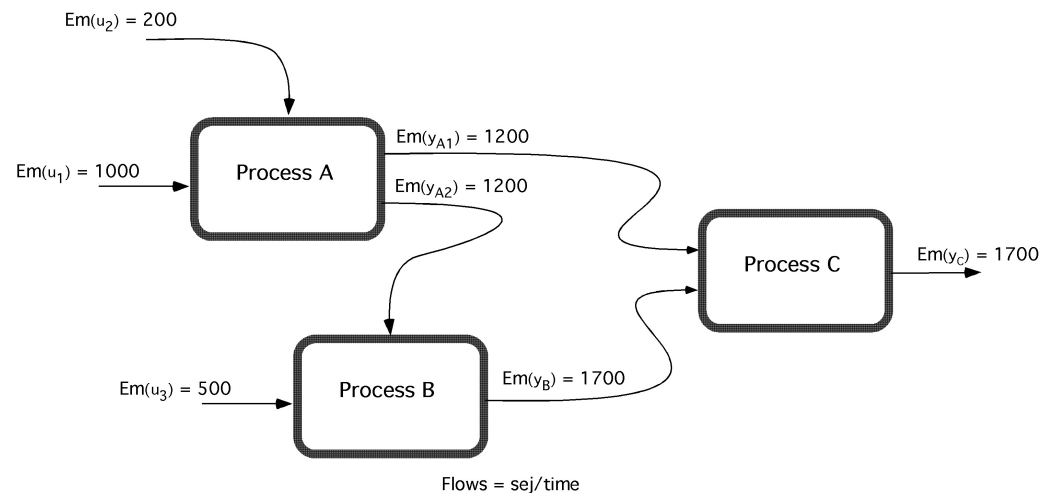
- *energy in feedbacks cannot be double counted*
- *co-products, when reunited cannot be added to equal a sum greater than the source energy from which they were derived.*



## Rule #5 – Double counting...

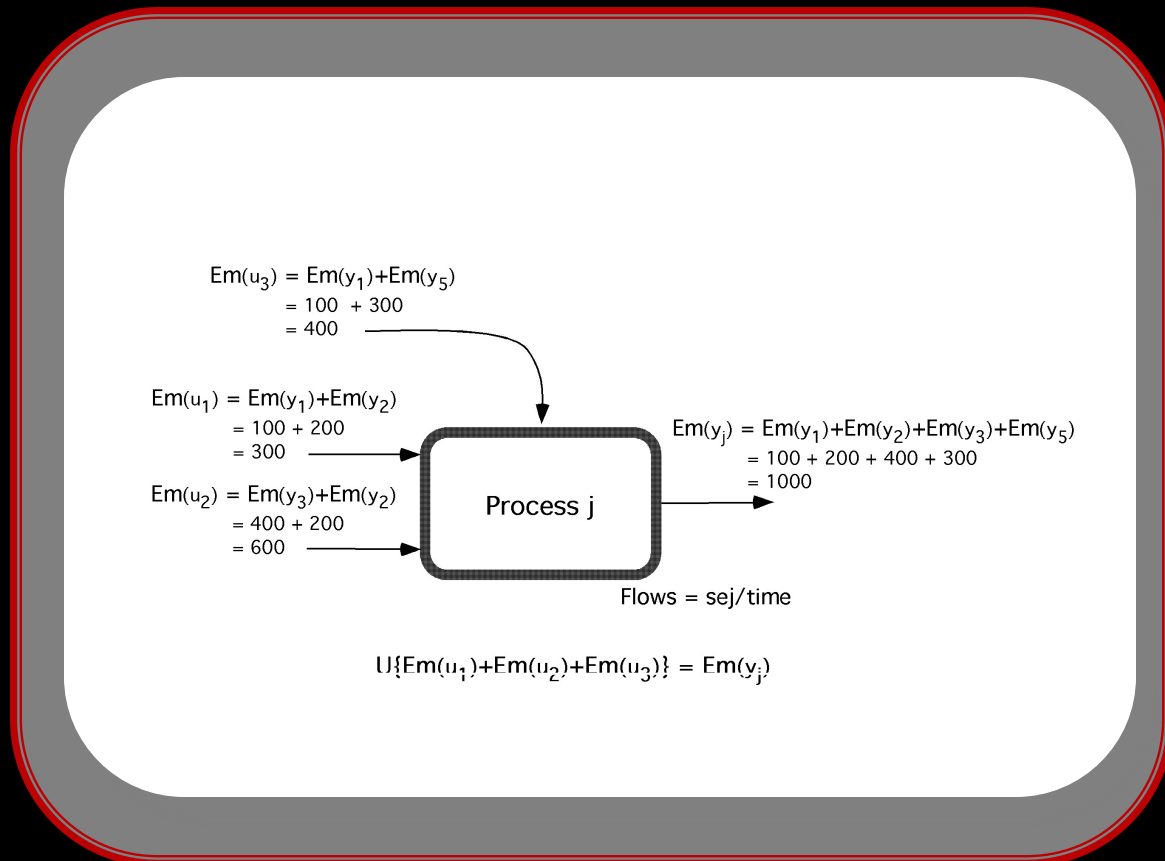
*Within a system, energy cannot be counted twice:*

- energy in feedbacks cannot be double counted*
- co-products, when reunited cannot be added to equal a sum greater than the source energy from which they were derived.*



## Rule #5 – Double counting (continued)...

*Only those emergy flows which make up inputs  $Em(u_1)$ ,  $Em(u_2)$ , and  $Em(u_3)$  that are distinct and independent are included in the output,  $Em(y_j)$ .*



## Rule #5 – Double counting (continued)...

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Set theory has a convenient way of denoting concept of independent flows using the union ( $\cup$ ) operation.

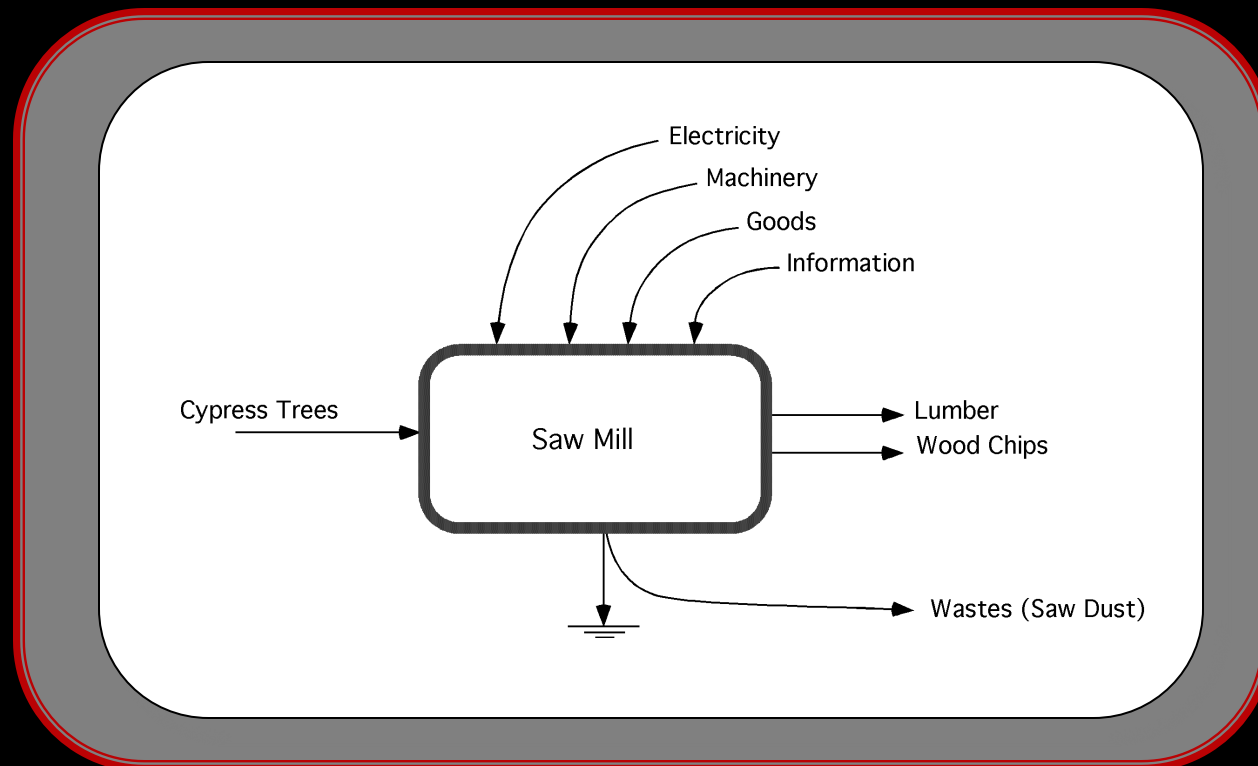
The union ( $\cup$ ) of a collection of sets is the set of all distinct elements in the collection.

For instance the union of the two sets  $\{1, 2, 3\}$  and  $\{2, 3, 4\}$  is  $\{1, 2, 3, 4\}$ . Only the elements of the two sets that are distinct are represented by their union.

$$\cup \{Em(u_1), Em(u_2), Em(u_3)\} = Em(y_j)$$

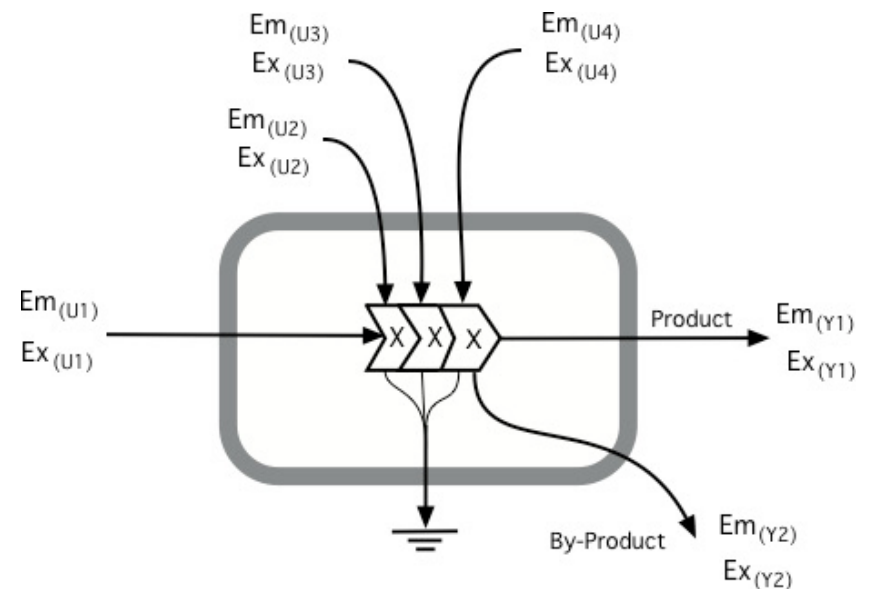
## Co-products vs. By-products

Co-products are products that are jointly produced and are up grades of the inputs, while a by-product is an incidental output (an output that is a down grade of the inputs).



## Rule #6: By-product flows...

A by-product is an incidental material or energy produced in a process that is a degraded form of the inputs

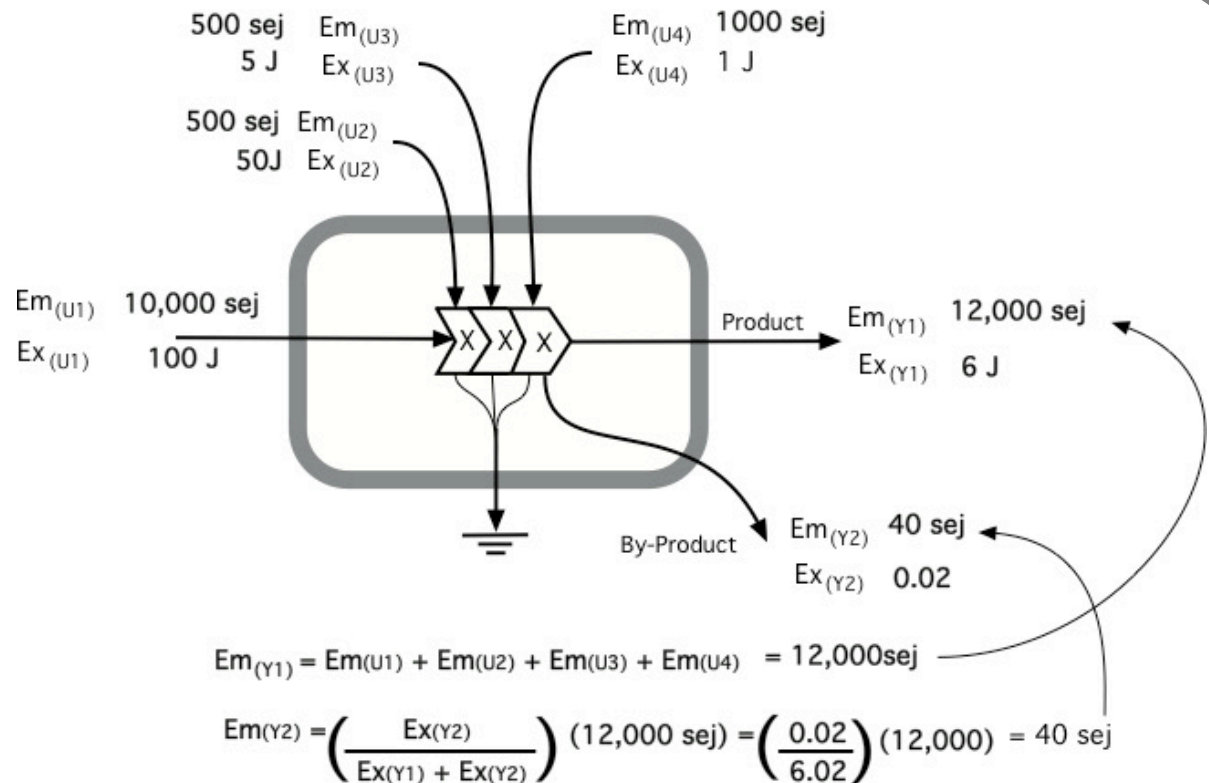


$$Em_{(y1)} = Em_{(u1)} + Em_{(u2)} + Em_{(u3)} + Em_{(u4)}$$

$$Em_{(y2)} = \frac{Ex_{(y2)}}{Ex_{(y1)} + Ex_{(y2)}} (Em_{(y1)})$$

## Rule #6: By-product flows...

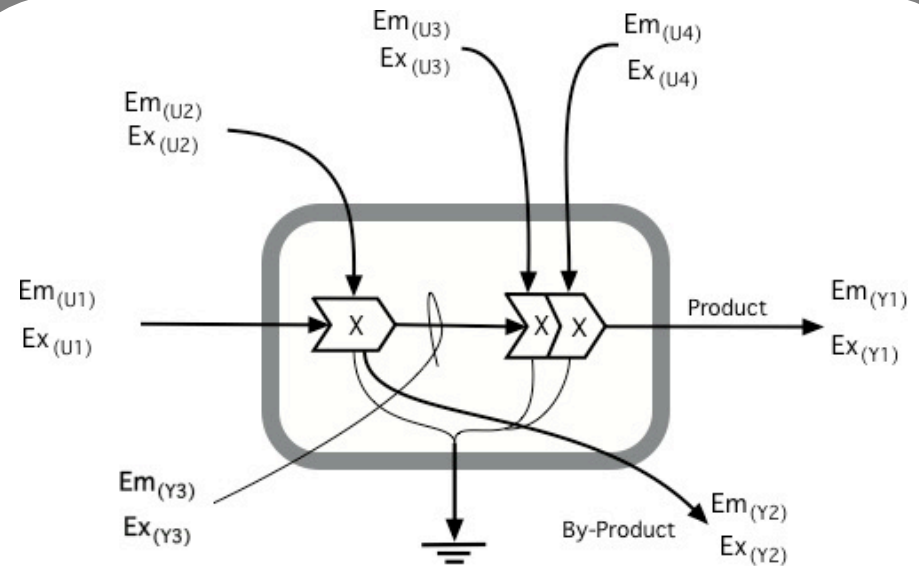
The energy of the by-product flow is assigned based on the percentage of the total exergy that is the exergy of the by-product flow





## Rule #6: By-product flows...

A by-product is an incidental material or energy produced in a process that is a degraded form of the inputs

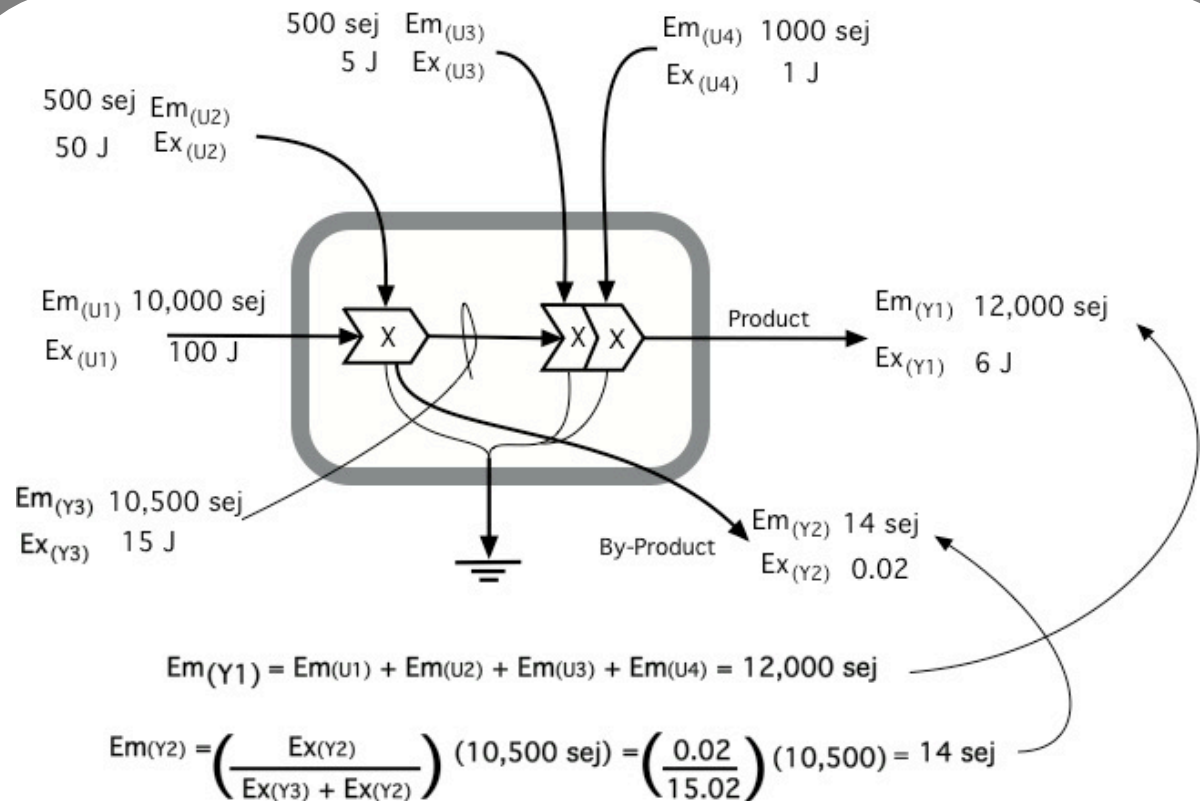


$$Em_{(y1)} = Em_{(u1)} + Em_{(u2)} + Em_{(u3)} + Em_{(u4)}$$

$$Em_{(y2)} = \left( \frac{Ex_{(y2)}}{Ex_{(y3)} + Ex_{(y2)}} \right)$$

## Rule #6: By-product flows...

The energy of the by-product flow is assigned based on the percentage of the total exergy that is the exergy of the by-product flow

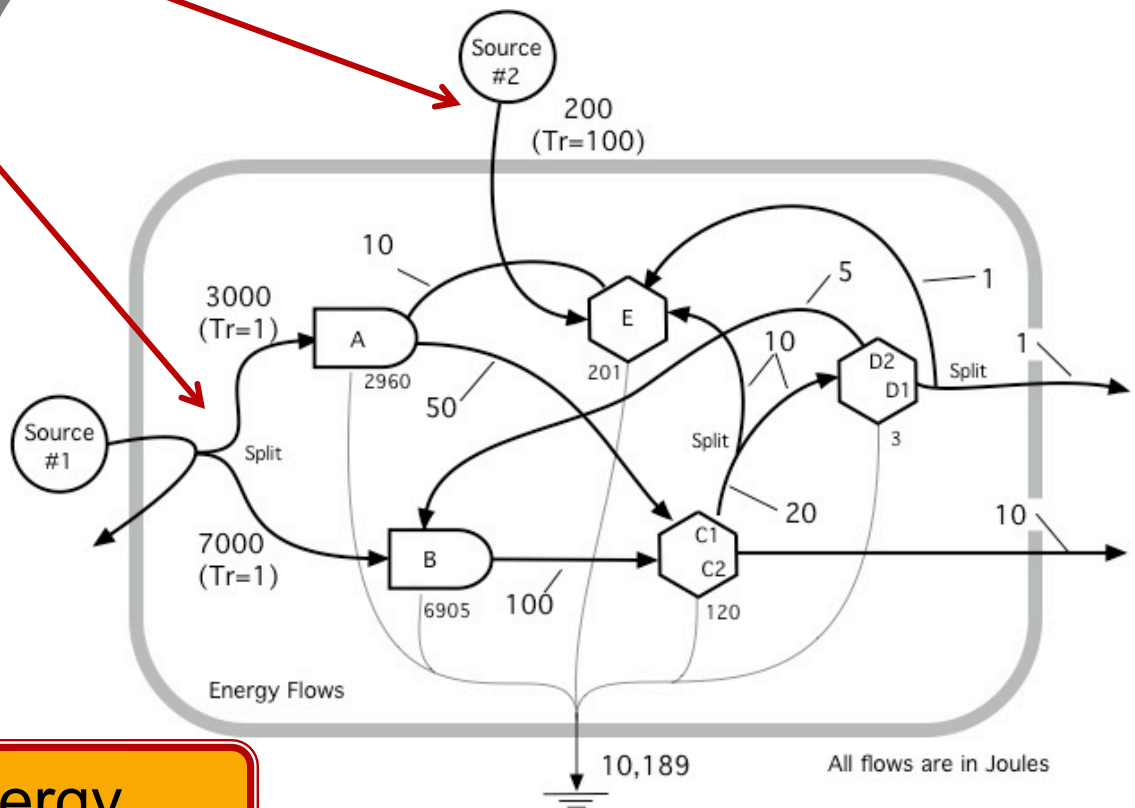


UEV = 100 sej/J

UEV = 1 sej/J

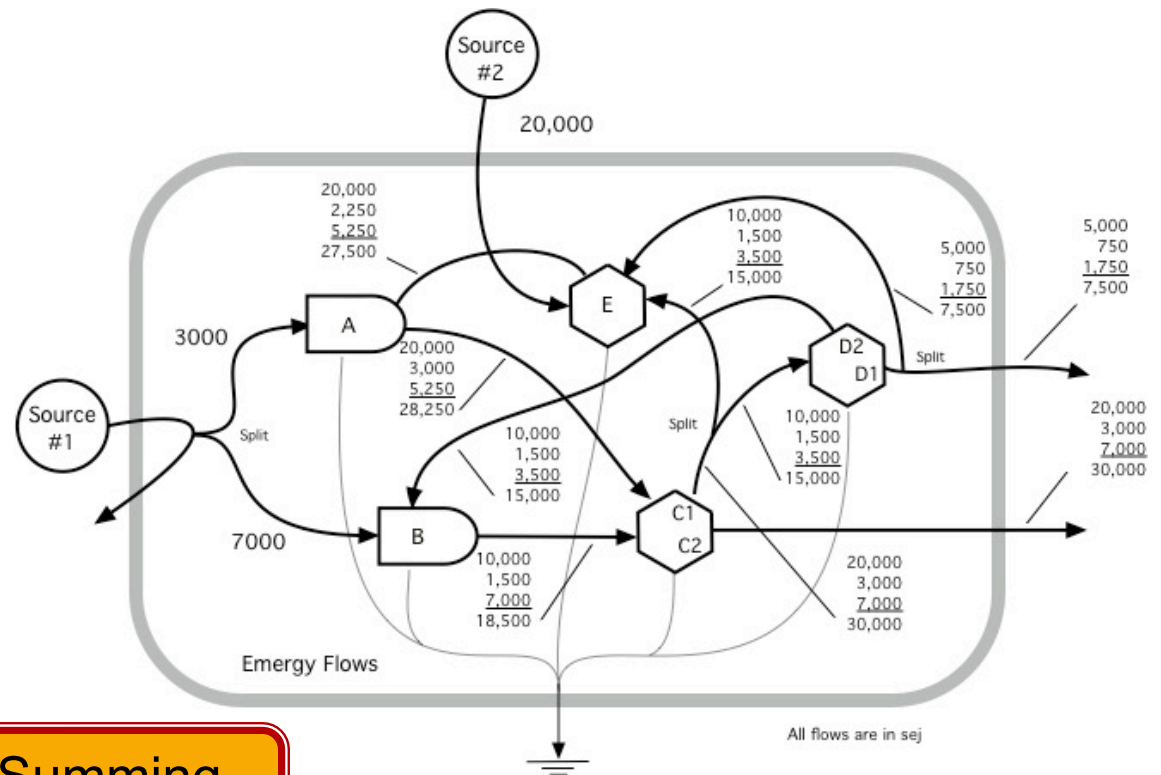
A more complex system example

...Splits, co-products, and "doublecounting"



Energy

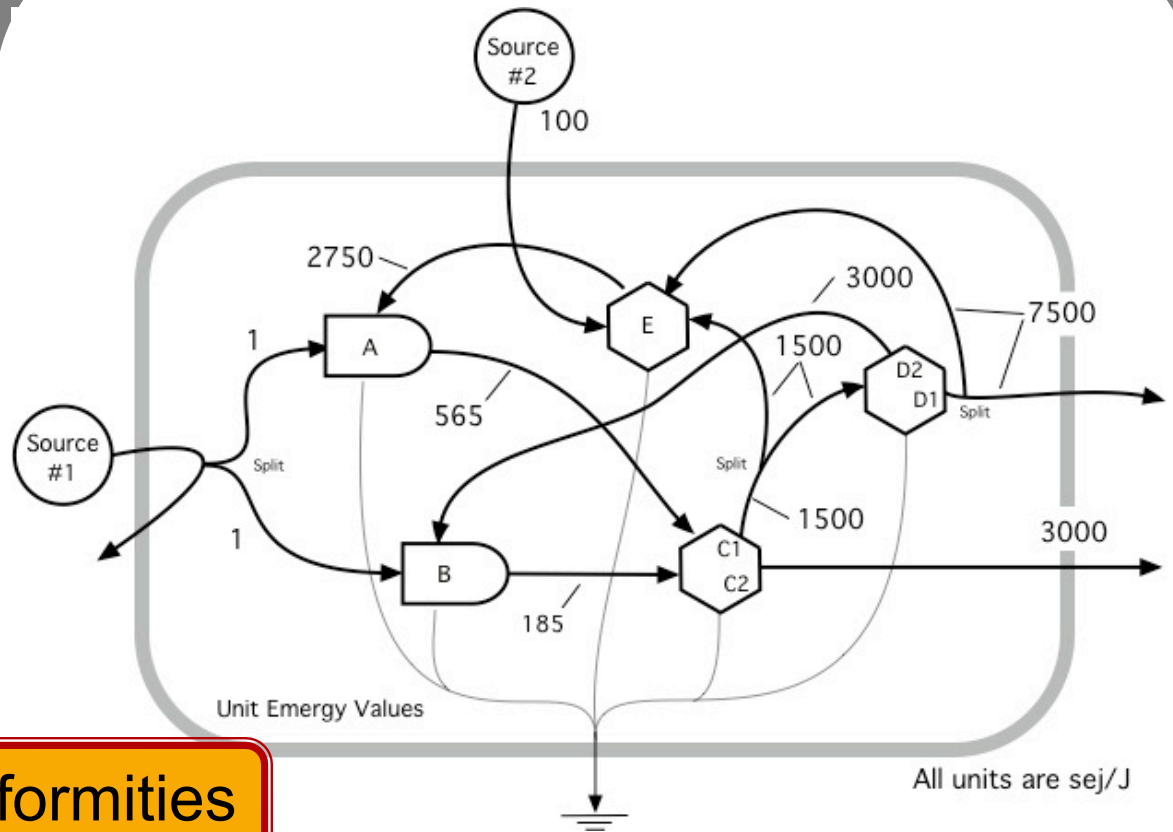
Track-Summing Method  
 - Track each source, in turn, and then sum the energy input to each component



Track Summing

# Resulting solar energy transformities

(Divide the energy on each pathway by the energy)

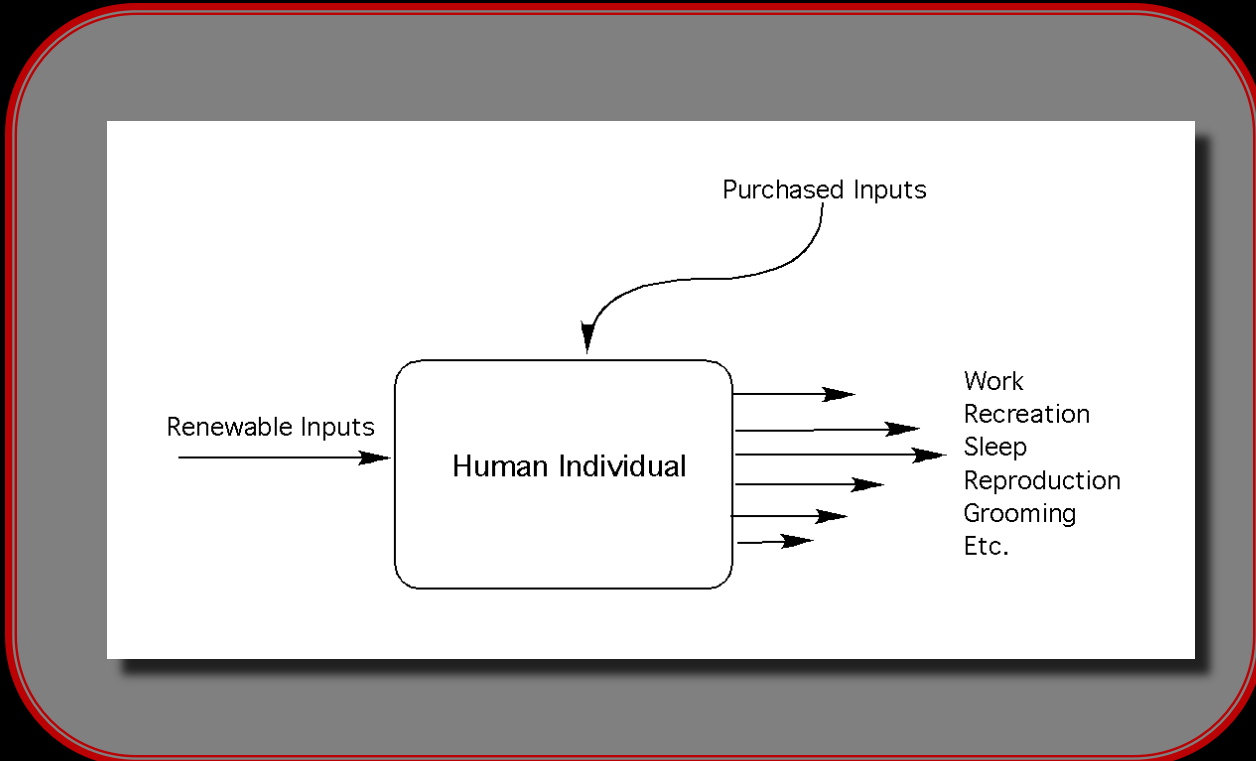


**Transformities**

# Theoretical Consideration...

## Human co-products and by-products

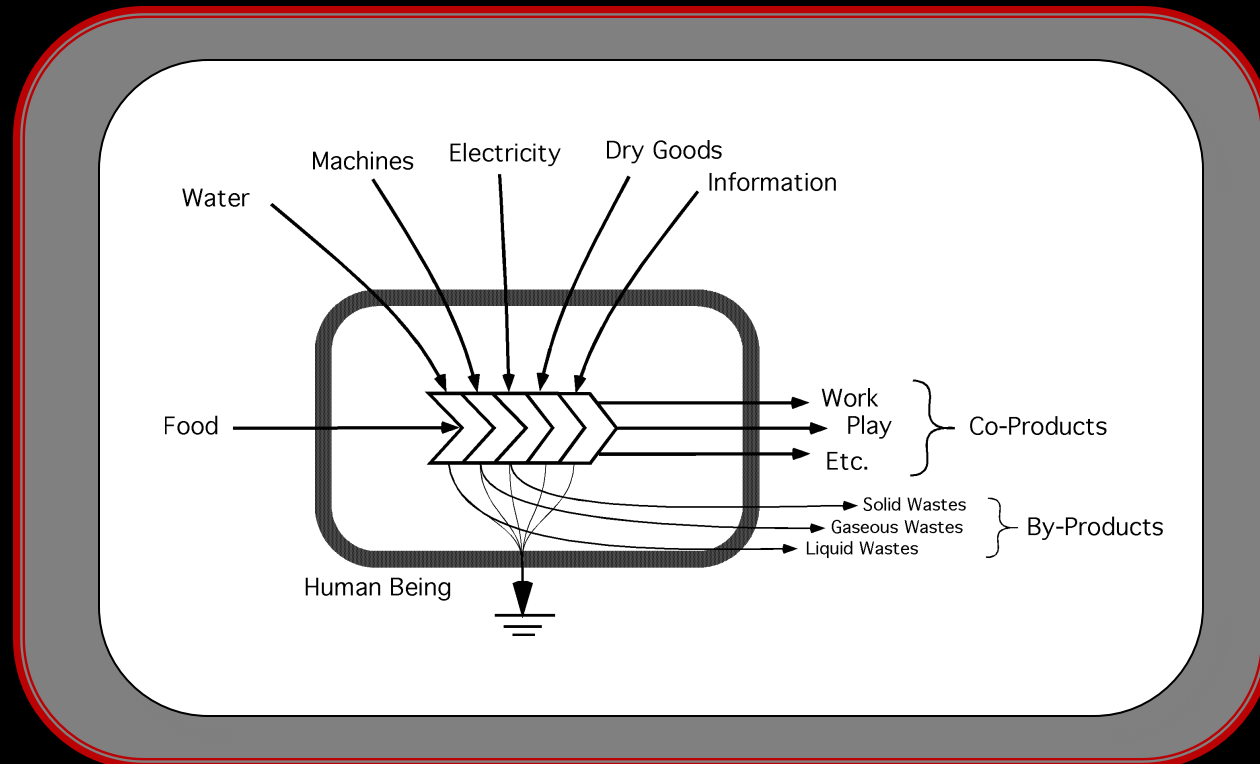
Clearly the outputs from the human individual are co-products



# Theoretical Consideration...

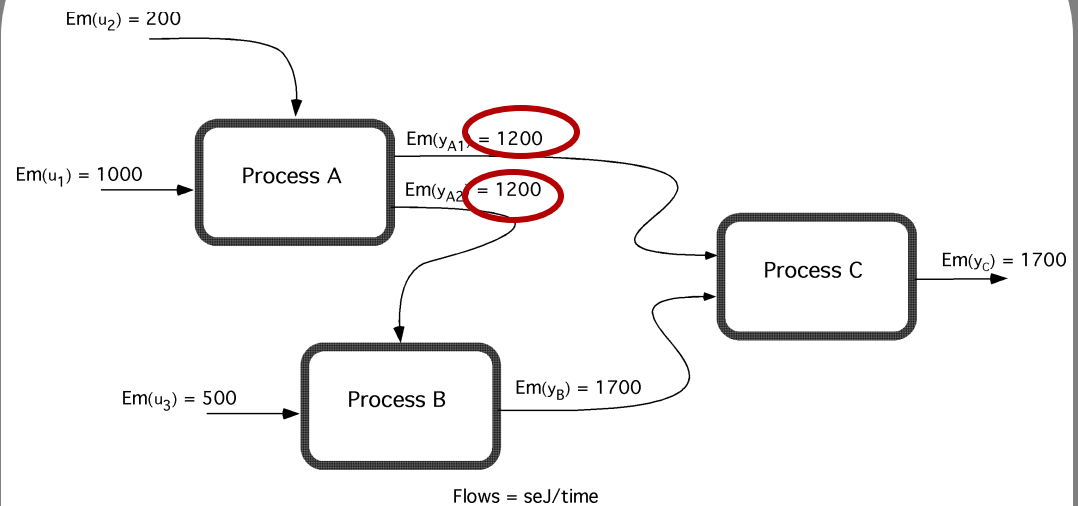
## Human co-products and by-products

...but what about by-products?



## Theoretical Consideration...

What if there is a delay in the system such that the bottom co-product inflow to Process B is not produced with the same energy as the top co-product?

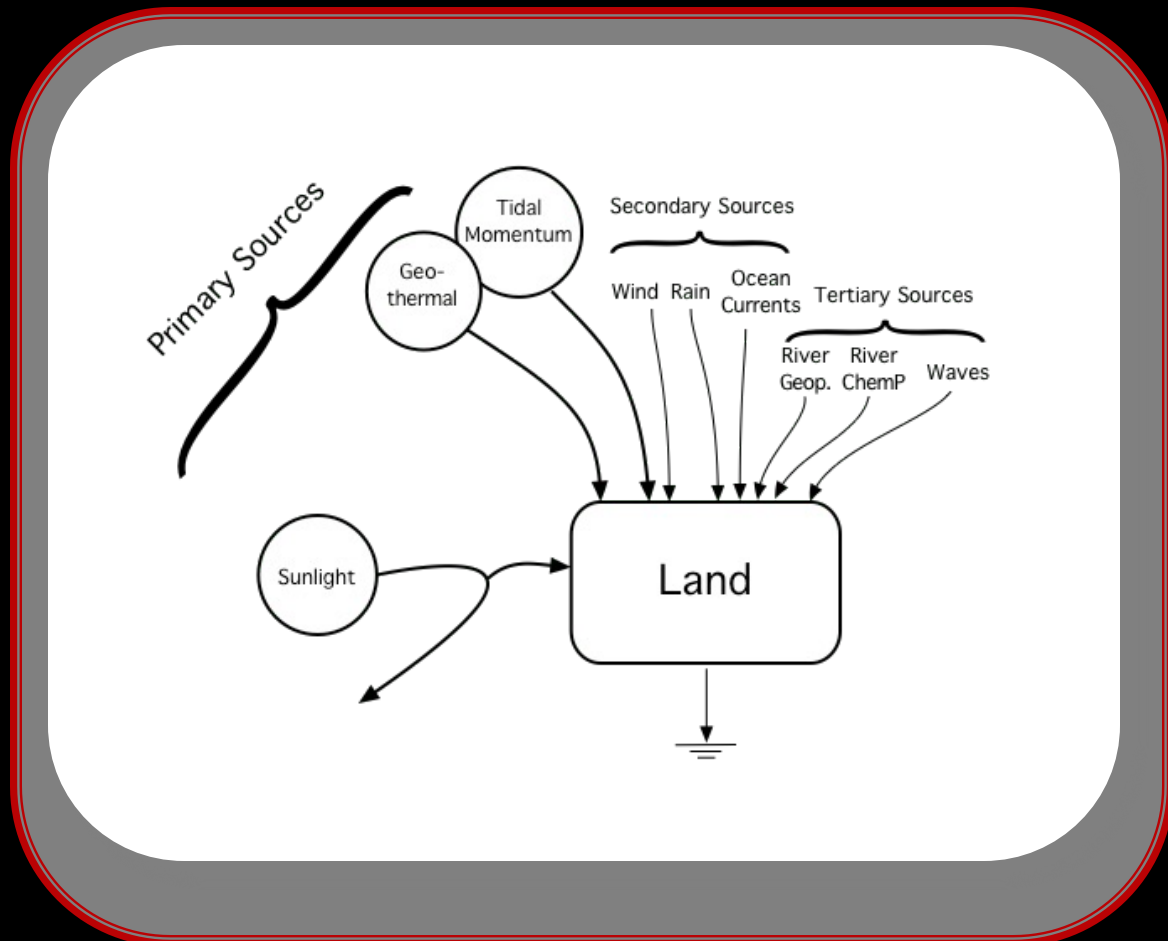


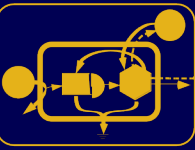


# IMPORTANT Consideration...

Input Emergy =

Maximum of Sum of the Primary vs. largest of the secondary & tertiary sources





Questions ?

Comments ?

Concerns?